

Family Support Materials

Probability and Sampling

Here are the video lesson summaries for Grade 7, Unit 8: Probability and Sampling. Each video highlights key concepts and vocabulary that students learn across one or more lessons in the unit. The content of these video lesson summaries is based on the written Lesson Summaries found at the end of lessons in the curriculum. The goal of these videos is to support students in reviewing and checking their understanding of important concepts and vocabulary. Here are some possible ways families can use these videos:

- Keep informed on concepts and vocabulary students are learning about in class.
- Watch with their student and pause at key points to predict what comes next or think up other examples of vocabulary terms (the bolded words).
- Consider following the Connecting to Other Units links to review the math concepts that led up to this unit or to preview where the concepts in this unit lead to in future units.

Grade 7, Unit 8: Probability and Sampling	Vimeo	YouTube
Video 1: Estimating Probabilities (Lessons 1–5)	Link	Link
Video 2: Multi-step Experiments (Lessons 6–10)	Link	Link
Video 3: Sampling (Lessons 11–14)	Link	Link
Video 4: Using Samples (Lessons 15–19)	Link	Link

Video 1

Video 'VLS G7U8V1 Estimating Probabilities (Lessons 1–5)' available here:
<https://player.vimeo.com/video/521004741>.

Video 2

Video 'VLS G7U8V2 Multi-step Experiments (Lessons 6–10)' available here:
<https://player.vimeo.com/video/521022437>.

Video 3

Video 'VLS G7U8V3 Sampling (Lessons 11–14)' available here: <https://player.vimeo.com/video/523876549>.

Video 4

Video 'VLS G7U8V4 Using Samples (Lessons 15–19)' available here: <https://player.vimeo.com/video/523185261>.

Probabilities of Single Step Events

Family Support Materials 1

This week your student will be working with probability. A **probability** is a number that represents how likely something is to happen. For example, think about flipping a coin.

- The probability that the coin lands somewhere is 1. That is certain.
- The probability that the coin lands heads up is $\frac{1}{2}$, or 0.5.
- The probability that the coin turns into a bottle of ketchup is 0. That is impossible.

Sometimes we can figure out an exact probability. For example, if we pick a random date, the chance that it is on a weekend is $\frac{2}{7}$, because 2 out of every 7 days fall on the weekend. Other times, we can estimate a probability based on what we have observed in the past.

Here is a task to try with your student:

People at a fishing contest are writing down the type of each fish they catch. Here are their results:

- Person 1: bass, catfish, catfish, bass, bass, bass
- Person 2: catfish, catfish, bass, bass, bass, bass, catfish, catfish, bass, catfish
- Person 3: bass, bass, bass, catfish, bass, bass, catfish, bass, catfish

1. Estimate the probability that the next fish that gets caught will be a bass.
2. Another person in the competition caught 5 fish. Predict how many of these fish were bass.
3. Before the competition, the lake was stocked with equal numbers of catfish and bass. Describe some possible reasons for why the results do not show a probability of $\frac{1}{2}$ for catching a bass.

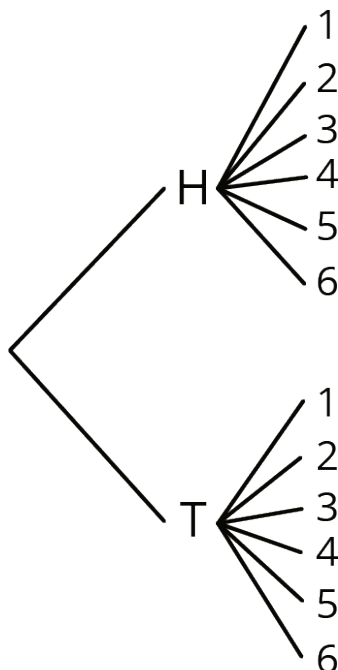
Solution:

1. About $\frac{15}{25}$, or 0.6, because of the 25 fish that have been caught, 15 of them were bass.
2. About 3 bass, because $\frac{3}{5} = 0.6$. It would also be reasonable if they caught 2 or 4 bass, out of their 5 fish.
3. There are many possible answers. For example:
 - Maybe the lures or bait they were using are more likely to catch bass.
 - With results from only 25 total fish caught, we can expect the results to vary a little from the exact probability.

Probabilities of Multi-step Events

Family Support Materials 2

To find an exact probability, it is important to know what outcomes are possible. For example, to show all the possible outcomes for flipping a coin and rolling a number cube, we can draw this tree diagram:



The branches on this tree diagram represent the 12 possible outcomes, from “heads 1” to “tails 6.” To find the probability of getting heads on the coin and an even number on the number cube, we can see that there are 3 ways this could happen (“heads 2”, “heads 4”, or “heads 6”) out of 12 possible outcomes. That means the probability is $\frac{3}{12}$, or 0.25.

Here is a task to try with your student:

A board game uses cards that say “forward” or “backward” and a spinner numbered from 1 to 5.

1. On their turn, a person picks a card and spins the spinner to find out which way and how far to move their piece. How many different outcomes are possible?
2. On their next turn, what is the probability that the person will:
 - a. get to move their piece forward 5 spaces?
 - b. have to move their piece backward some odd number of spaces?

Solution:

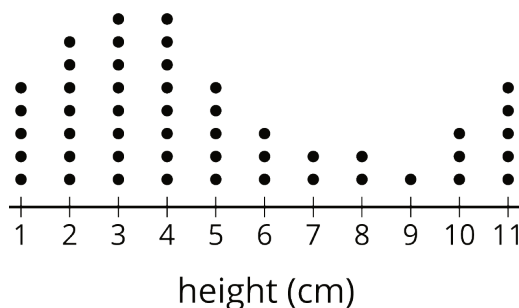
1. There are 10 possible outcomes (“forward 1”, “forward 2”, “forward 3”, “forward 4”, “forward 5”, “backward 1”, “backward 2”, “backward 3”, “backward 4”, or “backward 5”).
2.
 - a. $\frac{1}{10}$ or 0.1, because “forward 5” is 1 out of the 10 possibilities.
 - b. $\frac{3}{10}$ or 0.3, because there are 3 such possibilities (“backward 1”, “backward 3”, or “backward 5”)

Sampling

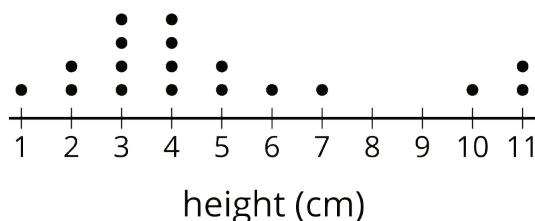
Family Support Materials 3

This week your student will be working with data. Sometimes we want to know information about a group, but the group is too large for us to be able to ask everyone. It can be useful to collect data from a **sample** (some of the group) of the **population** (the whole group). It is important for the sample to resemble the population.

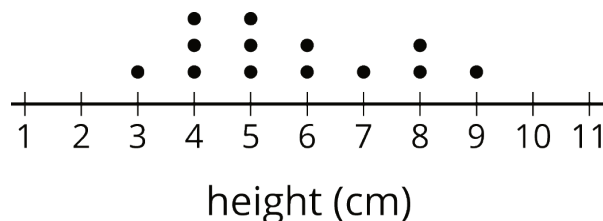
- For example, here is a dot plot showing a population: the height of 49 plants in a sprout garden.



- This sample is **representative** of the population, because it includes only a part of the data, but it still resembles the population in shape, center, and spread.



- This sample is not representative of the population. It has too many plant heights in the middle and not enough really short or really tall ones.



A sample that is selected at random is more likely to be representative of the population than a sample that was selected some other way.

Here is a task to try with your student:

A city council needs to know how many buildings in the city have lead paint, but they don't have enough time to test all 100,000 buildings in the city. They want to test a sample of buildings that will be representative of the population.

1. What would be a *bad* way to pick a sample of the buildings?

2. What would be a *good* way to pick a sample of the buildings?

Solution:

1. There are many possible answers.
 - Testing all the same type of buildings (like all the schools, or all the gas stations) would not lead to a representative sample of all the buildings in the city.
 - Testing buildings all in the same location, such as the buildings closest to city hall, would also be a bad way to get a sample.
 - Testing all the newest buildings would *bias* the sample towards buildings that don't have any lead paint.
 - Testing a small number of buildings, like 5 or 10, would also make it harder to use the sample to make predictions about the entire population.
2. To select a sample at random, they could put the addresses of all 100,000 buildings into a computer and have the computer select 50 addresses randomly from the list. Another possibility could be picking papers out a bag, but with so many buildings in the city, this method would be difficult.

Using Samples

Family Support Materials 4

We can use statistics from a sample (a part of the entire group) to estimate information about a population (the entire group). If the sample has more variability (is very spread out), we may not trust the estimate as much as we would if the numbers were closer together. For example, it would be easier to estimate the average height of all 3-year olds than all 40-year olds, because there is a wider range of adult heights.

We can also use samples to help predict whether there is a meaningful difference between two populations, or whether there is a lot of overlap in the data.

Here is a task to try with your student:

Students from seventh grade and ninth grade were selected at random to answer the question, "How many pencils do you have with you right now?" Here are the results:

how many pencils each seventh grade student had

4	1	2	5	2	1	1	2	3	3
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how many pencils each ninth grade student had

9	4	1	14	6	2	0	8	2	5
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1. Use the sample data to estimate the mean (average) number of pencils carried by:
 - a. all the seventh grade students in the whole school.
 - b. all the ninth grade students in the whole school.

2. Which sample had more variability? What does this tell you about your estimates in the previous question?

3. A student, who was not in the survey, has 5 pencils with them. If this is all you know, can you predict which grade they are in?

Solution:

1. Since the samples were selected at random, we predict they will represent the whole population fairly well.
 - a. About 2.4 pencils for all seventh graders, because the mean of the sample is $(4 + 1 + 2 + 5 + 2 + 1 + 1 + 2 + 3 + 3) \div 10$ or 2.4 pencils.
 - b. About 5.1 pencils for all ninth graders, because the mean of the sample is $(9 + 4 + 1 + 14 + 6 + 2 + 0 + 8 + 2 + 5) \div 10$ or 5.1 pencils.
2. The survey of ninth graders had more variability. Those numbers were more spread out, so I trust my estimate for seventh grade more than I trust my estimate for ninth grade.
3. There are many possible answers. For example:
 - Since they only asked 10 students from each grade, it is hard to predict. It would help if they could ask more students.
 - The student is probably in ninth grade, because 5 is closer to the sample mean from ninth grade than from seventh grade.
 - The student could possibly be in seventh grade, because at least one student in seventh grade has 5 pencils.