## Unit 7 Lesson 11: A New Way to Measure Angles

### 1 A One-Unit Radius (Warm up)

#### Student Task Statement

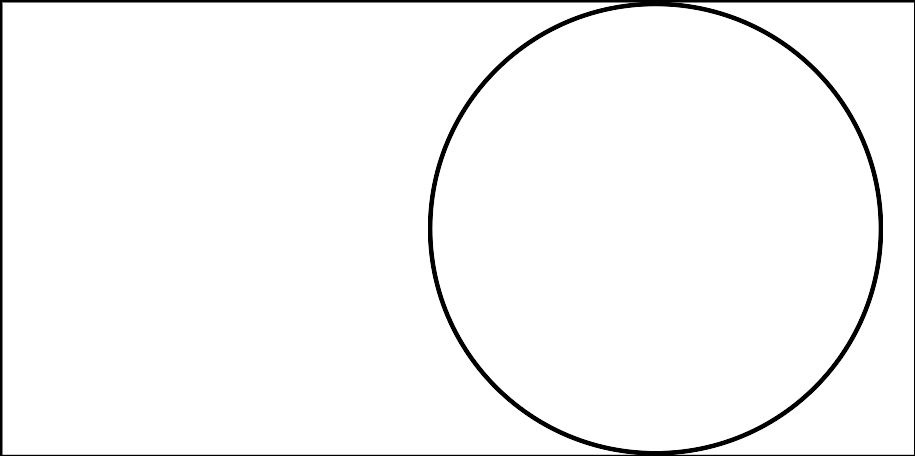
A circle has radius 1 unit. Find the length of the arc defined by each of these central angles. Give your answers in terms of .

1. 180 degrees
2. 45 degrees
3. 270 degrees
4. 225 degrees
5. 360 degrees

### 2 A Constant Ratio

#### Student Task Statement

Diego and Lin are looking at 2 circles.



Diego says, “It seems like for a given central angle, the arc length is proportional to the radius. That is, the ratio has the same value as the ratio  because they have the same central angle measure. Can we prove that this is true?”

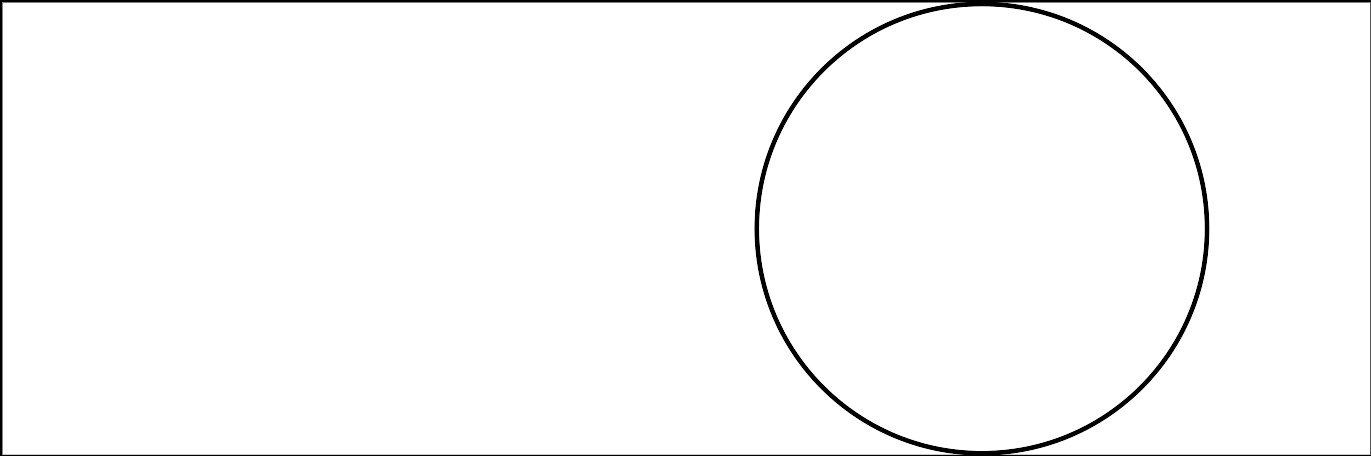
Lin says, “The big circle is a dilation of the small circle. If is the scale factor, then .”

Diego says, “The arc length in the small circle is . In the large circle, it’s . We can rewrite that as . So .”

Lin says, “Okay, from here I can show that  and are equivalent.”

1. How does Lin know that the big circle is a dilation of the small circle?
2. How does Lin know that ?
3. Why could Diego write ?
4. When Diego says that , what does that mean in words?
5. Why could Diego say that ?
6. How can Lin show that ?

#### Activity Synthesis



### 3 Defining Radians

#### Student Task Statement

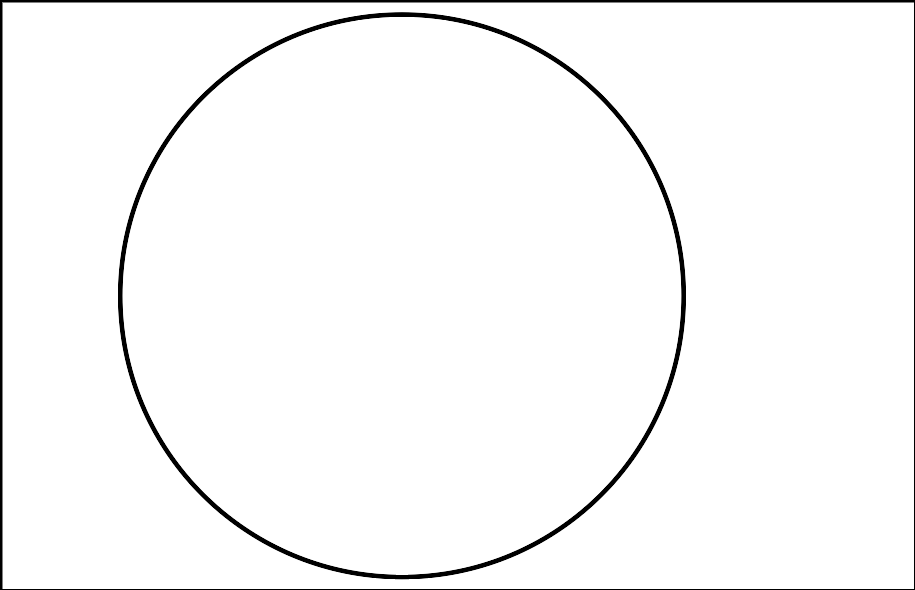
Suppose we have a circle that has a central angle. The **radian** measure of the angle is the ratio of the length of the arc defined by the angle to the circle’s radius. That is, .

1. The image shows a circle with radius 1 unit.

* 
  1. Cut a piece of string that is the length of the radius of this circle.
  2. Use the string to mark an arc on the circle that is the same length as the radius.
  3. Draw the central angle defined by the arc.
  4. Use the definition of radian to calculate the radian measure of the central angle you drew.

1. Draw a 180 degree central angle (a diameter) in the circle. Use your 1-unit piece of string to measure the approximate length of the arc defined by this angle.
2. Calculate the radian measure of the 180 degree angle. Give your answer both in terms of and as a decimal rounded to the nearest hundredth.
3. Calculate the radian measure of a 360 degree angle.

#### Images for Activity Synthesis





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