## Unit 5 Lesson 12: Reasoning about Exponential Graphs (Part 1)

### 1 Spending Gift Money (Warm up)

#### Student Task Statement

Jada received a gift of $180. In the first week, she spent a third of the gift money. She continues spending a third of what is left each week thereafter. Which equation best represents the amount of gift money $g$, in dollars, she has after $t$ weeks? Be prepared to explain your reasoning.

1. $g=180−\frac{1}{3}t$
2. $g=180⋅\left(\frac{1}{3}\right)^{t}$
3. $g=\frac{1}{3}⋅180^{t}$
4. $g=180⋅\left(\frac{2}{3}\right)^{t}$

### 2 Equations and Their Graphs

#### Student Task Statement

1. Each of the following functions $f$, $g$$,$ $h$, and $j$ represents the amount of money in a bank account, in dollars, as a function of time $x$, in years. They are each written in form $m(x)=a⋅b^{x}$.
$f(x)=50⋅2^{x}$
$g(x)=50⋅3^{x}$
$h(x)=50⋅\left(\frac{3}{2}\right)^{x}$
$j(x)=50⋅(0.5)^{x}$
	1. Use graphing technology to graph each function on the same coordinate plane.
	2. Explain how changing the value of $b$ changes the graph.
2. Here are equations defining functions $p$, $q$, and $r$. They are also written in the form $m(x)=a⋅b^{x}$.
$p(x)=10⋅4^{x}$
$q(x)=40⋅4^{x}$
$r(x)=100⋅4^{x}$
	1. Use graphing technology to graph each function and check your prediction.
	2. Explain how changing the value of $a$ changes the graph.

### 3 Graphs Representing Exponential Decay

#### Student Task Statement

$m(x)=200⋅\left(\frac{1}{4}\right)^{x}$
$n(x)=200⋅\left(\frac{1}{2}\right)^{x}$
$p(x)=200⋅\left(\frac{3}{4}\right)^{x}$
$q(x)=200⋅\left(\frac{7}{8}\right)^{x}$



1. Match each equation with a graph. Be prepared to explain your reasoning.
2. Functions $f$ and $g$ are defined by these two equations: $f(x)=1,​000⋅\left(\frac{1}{10}\right)^{x}$ and $g(x)=1,​000⋅\left(\frac{9}{10}\right)^{x}$.
	1. Which function is decaying more quickly? Explain your reasoning.
	2. Use graphing technology to verify your response.



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