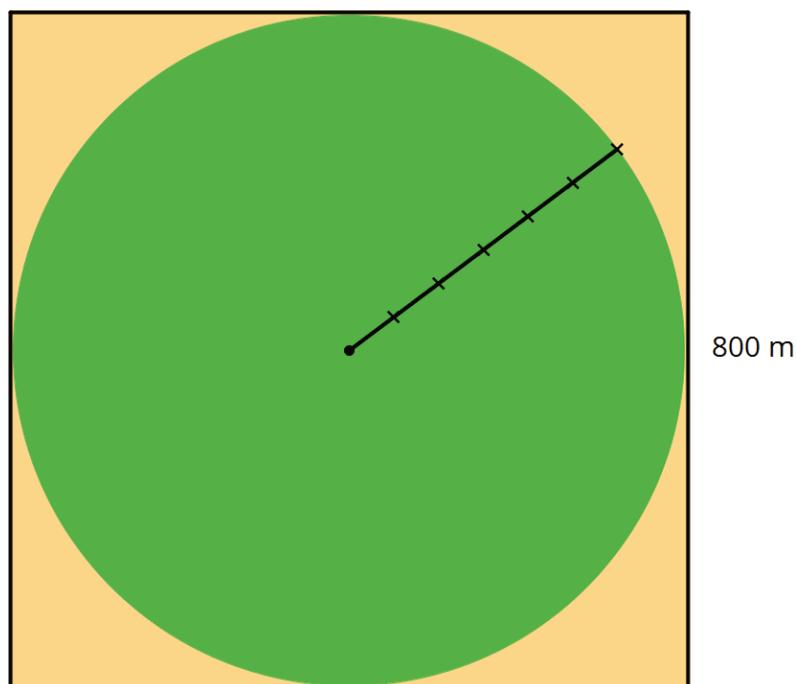


## Lesson 16: Applying Area of Circles

Let's find the areas of shapes made up of circles.

### 16.1: Still Irrigating the Field

The area of this field is about  $500,000 \text{ m}^2$ . What is the field's area to the nearest square meter? Assume that the side lengths of the square are exactly 800 m.

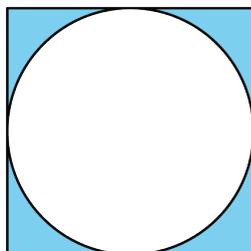


- $502,400 \text{ m}^2$
- $502,640 \text{ m}^2$
- $502,655 \text{ m}^2$
- $502,656 \text{ m}^2$
- $502,857 \text{ m}^2$

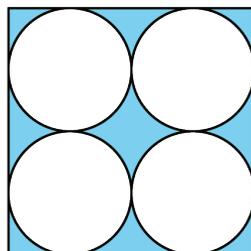
## 16.2: Comparing Areas Made of Circles

1. Each square has a side length of 12 units. Compare the areas of the shaded regions in the 3 figures. Which figure has the largest shaded region? Explain or show your reasoning.

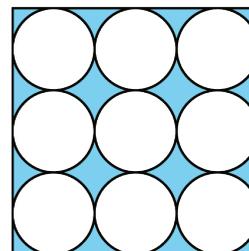
A



B

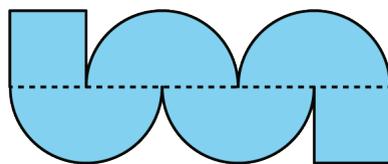


C

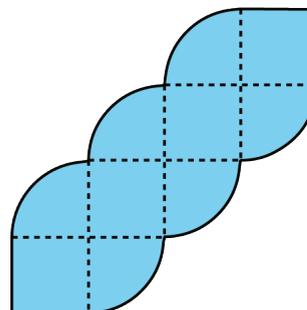


2. Each square in Figures D and E has a side length of 1 unit. Compare the area of the two figures. Which figure has more area? How much more? Explain or show your reasoning.

D



E

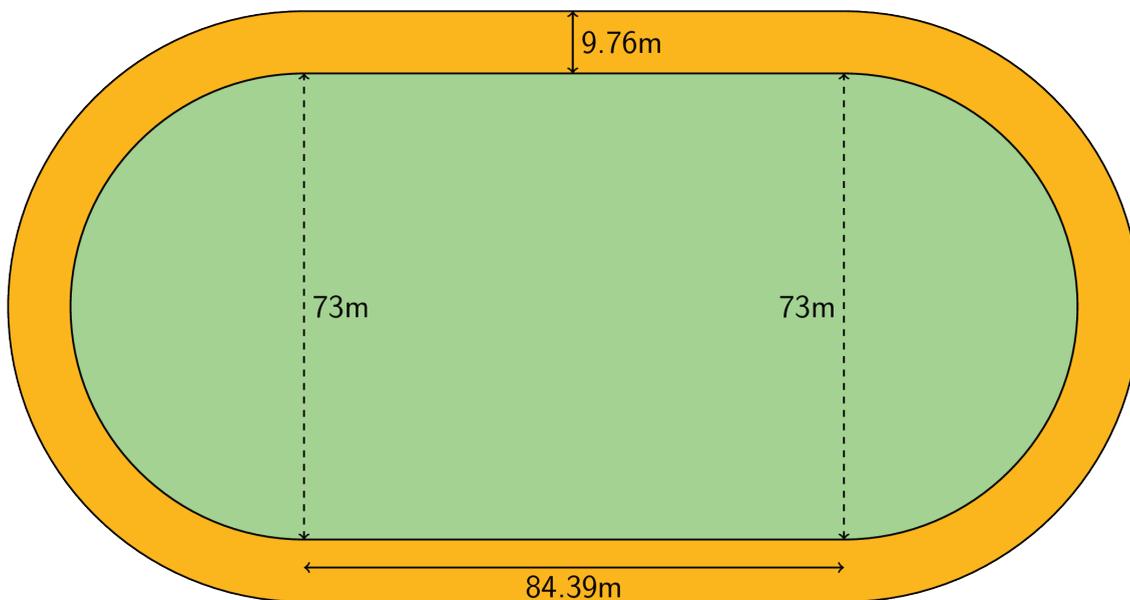


### Are you ready for more?

Which figure has a longer perimeter, Figure D or Figure E? How much longer?

### 16.3: The Running Track Revisited

The field inside a running track is made up of a rectangle 84.39 m long and 73 m wide, together with a half-circle at each end. The running lanes are 9.76 m wide all the way around.



What is the area of the running track that goes around the field? Explain or show your reasoning.

## Lesson 16 Summary

The relationship between  $A$ , the area of a circle, and  $r$ , its radius, is  $A = \pi r^2$ . We can use this to find the area of a circle if we know the radius. For example, if a circle has a radius of 10 cm, then the area is  $\pi \cdot 10^2$  or  $100\pi$  cm<sup>2</sup>. We can also use the formula to find the radius of a circle if we know the area. For example, if a circle has an area of  $49\pi$  m<sup>2</sup> then its radius is 7 m and its diameter is 14 m.

Sometimes instead of leaving  $\pi$  in expressions for the area, a numerical approximation can be helpful. For the examples above, a circle of radius 10 cm has area about 314 cm<sup>2</sup>. In a similar way, a circle with area 154 m<sup>2</sup> has radius about 7 m.

We can also figure out the area of a fraction of a circle. For example, the figure shows a circle divided into 3 pieces of equal area. The shaded part has an area of  $\frac{1}{3}\pi r^2$ .

