

Family Support Materials

Functions and Volume

Here are the video lesson summaries for Grade 8, Unit 5: Functions and Volume. Each video highlights key concepts and vocabulary that students learn across one or more lessons in the unit. The content of these video lesson summaries is based on the written Lesson Summaries found at the end of lessons in the curriculum. The goal of these videos is to support students in reviewing and checking their understanding of important concepts and vocabulary. Here are some possible ways families can use these videos:

- Keep informed on concepts and vocabulary students are learning about in class.
- Watch with their student and pause at key points to predict what comes next or think up other examples of vocabulary terms (the bolded words).
- Consider following the Connecting to Other Units links to review the math concepts that led up to this unit or to preview where the concepts in this unit lead to in future units.

Grade 8, Unit 5: Functions and Volume	Vimeo	YouTube
Video 1: Inputs and Outputs (Lessons 1-3)	Link	Link
Video 2: Representing and Interpreting Functions (Lessons 4-7)	Link	Link
Video 3: Linear Functions and Rates of Change (Lessons 8-10)	Link	Link
Video 4: Cylinders and Cones (Lessons 11-16)	Link	Link
Video 5: Spheres (Lessons 19-21)	Link	Link

Video 1

Video 'VLS G8U5V1 Inputs and Outputs (Lessons 1–3)' available here:
<https://player.vimeo.com/video/493392446>.

Video 2

Video 'VLS G8U5V2 Representing and Interpreting Functions (Lessons 4–7)' available here:
<https://player.vimeo.com/video/498502033>.

Video 3

Video 'VLS G8U5V3 Linear Functions and Rates of Change (Lessons 8–10)' available here:
<https://player.vimeo.com/video/490206352>.

Video 4

Video 'VLS G8U5V4 Cylinders and Cones (Lessons 11–16)' available here:
<https://player.vimeo.com/video/493397357>.

Video 5

Video 'VLS G8U5V5 Spheres (Lessons 19–21)' available here: <https://player.vimeo.com/video/498158048>.

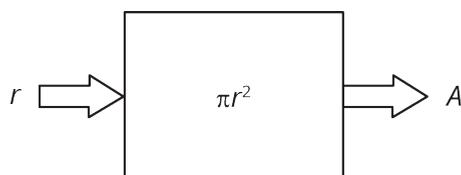
Inputs and Outputs

Family Support Materials 1

This week, your student will be working with **functions**. A function is a rule that produces a single output for a given input.

Not all rules are functions. For example, here’s a rule: the input is “first letter of the month” and the output is “the month.” If the input is J, what is the output? A function must give a single output, but in this case the output of this rule could be January, June, or July, so the rule is not a function.

Here is an example of a rule that is a function: input a number, square it, then multiply the result by π . Using r for the input and A for the output, we can draw a diagram to represent the function:



We could also represent this function with an equation, $A = \pi r^2$. We say that the input of the function, r , is the **independent variable** and the output of the function, A , is the **dependent variable**. We can choose any value for r , and then the value of A depends on the value of r . We could also represent this function with a table or as a graph. Depending on the question we investigate, different representations have different advantages. You may recognize this rule and know that the area of a circle depends on its radius.

Here is a task to try with your student:

Jada can buy peanuts for \$0.20 per ounce and raisins for \$0.25 per ounce. She has \$12 to spend on peanuts and raisins to make trail mix for her hiking group.

1. How much would 10 ounces of peanuts and 16 ounces of raisins cost? How much money would Jada have left?
2. Using p for pounds of peanuts and r for pounds of raisins, an equation relating how much of each they buy for a total of \$12 is $0.2p + 0.25r = 12$. If Jada wants 20 ounces of raisins, how many ounces of peanuts can she afford?
3. Jada knows she can rewrite the equation as $r = 48 - 0.8p$. In Jada’s equation, which is the independent variable? Which is the dependent variable?

Solution:

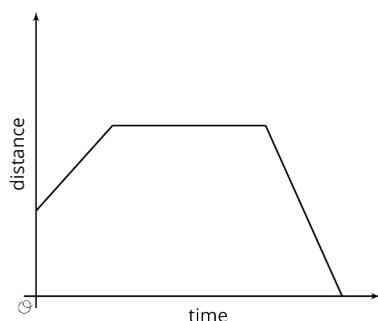
1. 10 ounces of peanuts would cost \$2 since $0.2 \cdot 10 = 2$. 16 ounces of raisins would cost \$4 since $0.25 \cdot 16 = 4$. Together, they would cost Jada \$6, leaving her with \$6.
2. 35 ounces of peanuts. If Jada wants 20 ounces of raisins, then $0.2p + 0.25 \cdot 20 = 12$ must be true, which means $p = 35$.
3. p is the independent variable and r is the dependent variable for Jada's equation.

Linear Functions and Rates of Change

Family Support Materials 2

This week, your student will be working with graphs of functions. The graph of a function is all the pairs (input, output), plotted in the coordinate plane. By convention, we always put the input first, which means the inputs are represented on the horizontal axis and the outputs on the vertical axis.

For a graph representing a context, it is important to specify the quantities represented on each axis. For example this graph shows Elena’s distance as a function of time. If it is distance from home, then Elena starts at some distance from home (maybe at her friend’s house), moves further away from her home (maybe to a park), stays there a while, and then returns home. If it is distance from school, the story is different.

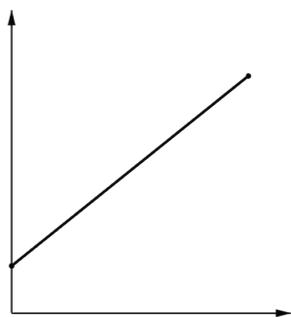


The story also changes depending on the scale on the axes: is distance measured in miles and time in hours, or is distance measured in meters and time in seconds?

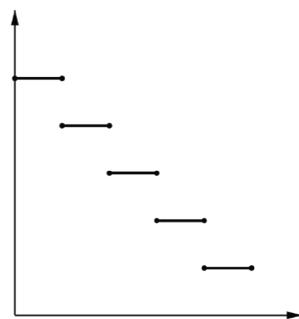
Here is a task to try with your student:

Match each of the following situations with a graph (you can use a graph multiple times). Define possible inputs and outputs, and label the axes.

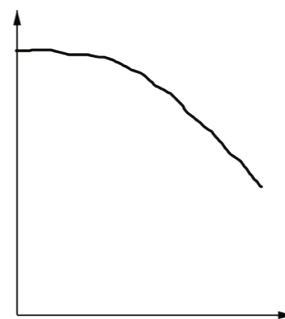
1. Noah pours the same amount of milk from a bottle every morning.
2. A plant grows the same amount every week.
3. The day started very warm but then it got colder.
4. A cylindrical glass contains some partially melted ice. The more water you pour in, the higher the water level.



A



B



C

Solution:

1. Graph B, input is time in days, output is amount of milk in the bottle
2. Graph A, input is time in weeks, output is height of plant
3. Graph C, input is time in hours, output is temperature
4. Graph A, input is volume of water, output is height of water

In each case, the horizontal axis is labeled with the input, and the vertical axis is labeled with the output.

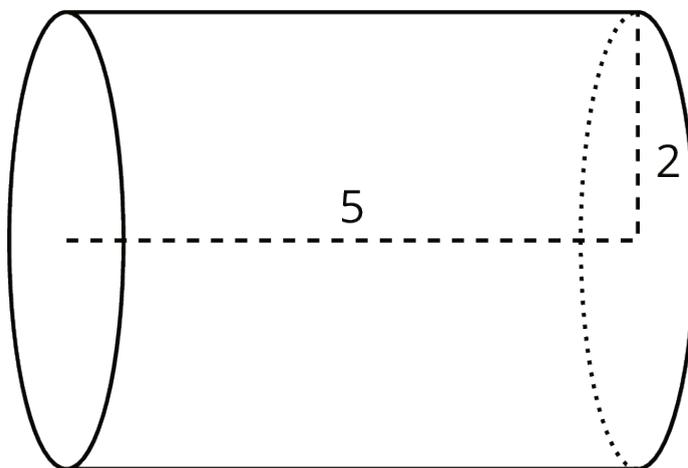
Cylinders and Cones

Family Support Materials 3

This week your student will be working with volumes of three-dimensional objects. We can determine the volume of a cylinder with radius r and height h using two ideas that we've seen before:

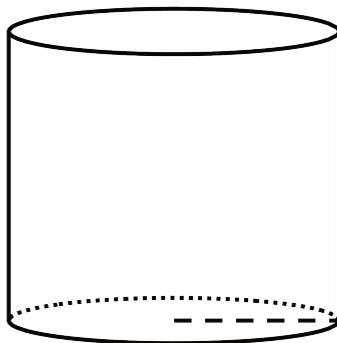
- The volume of a rectangular prism is a result of multiplying the area of its base by its height.
- The base of the cylinder is a circle with radius r , so the base area is πr^2 .

Just like a rectangular prism, the volume of a cylinder is the area of the base times the height. For example, let's say we have a cylinder whose radius is 2 cm and whose height is 5 cm like the one shown here:



The base has an area of $\pi 2^2 = 4\pi \text{ cm}^2$. Using this, we can calculate the volume to be $20\pi \text{ cm}^3$ since $4\pi \cdot 5 = 20\pi$. If we use 3.14 as an approximation for π , we can say that the volume of the cylinder is approximately 62.8 cm^3 . Students will also investigate the volume of cones and how their volume is related to the volume of a cylinder with the same radius and height.

Here is a task to try with your student:



This cylinder has a height and radius of 5 cm. Leave your answers in terms of π .

1. What is the diameter of the base?
2. What is the area of the base?
3. What is the volume of the cylinder?

Solution:

1. 10 cm. The diameter is $2 \cdot r$, and $2 \cdot 5 = 10$.
2. $25\pi \text{ cm}^2$. The area is π times the radius squared, or $5^2 \cdot \pi$.
3. $125\pi \text{ cm}^3$. The volume is the area of the base times the height. The area of the base here is 25π , so the volume is $125\pi \text{ cm}^3$ since $25\pi \cdot 5 = 125\pi$.

Dimensions and Spheres

Family Support Materials 4

This week, your student will compare the volumes of different objects. Many common objects, from water bottles to buildings to balloons, are similar in shape to rectangular prisms, cylinders, cones, and spheres—or even combinations of these shapes. We can use the volume formulas for these shapes to compare the volume of different types of objects.

For example, let's say we want to know which has more volume: a cube-shaped box with an edge length of 3 centimeters or a sphere with a radius of 2 centimeters.

The volume of the cube is 27 cubic centimeters since $\text{edge}^3 = 3^3 = 27$. The volume of the sphere is about 33.51 cubic centimeters since $\frac{4}{3}\pi \cdot \text{radius}^3 = \frac{4}{3}\pi \cdot 2^3 \approx 33.51$. Therefore, we can tell that the cube-shaped box holds less than the sphere.

Here is a task to try with your student:

A globe fits tightly inside a cubic box. The box has an edge length of 8 cm.

1. What is the volume of the box?
2. Estimate the volume of the globe: is it more or less than the volume of the box? How can you tell?
3. What is the diameter of the globe? The radius?
4. The formula for the volume of a sphere (like a globe) is $V = \frac{4}{3}\pi r^3$. What is the actual volume of the sphere? How close was your estimate in the previous problem?

Solution:

1. 512 cm^3 . The box is a cube, so its volume is 8^3 cubic centimeters.
2. Answers vary. The number should be less than 512 cm^3 since the volume of the globe must be less than the volume of the box. Possible explanation: it fits entirely inside the box, so it takes up less space. Since you can fit the globe inside the box and there is still space left over, the box has more volume.
3. Since the globe fits tightly inside the cubic box, the diameter of the globe must be the same as the edge length of the box, 8 cm. This means the radius is 4 cm.

4. $\frac{256}{3}\pi$ or about 268 cm^3 . Since the side length of the cube is 8 cm, the radius of the globe is half of that, or 4 cm. The volume of the globe is therefore $\frac{4}{3}\pi \cdot 4^3 = \frac{256}{3}\pi$.