

# Lesson 1: Growing and Shrinking

- Let's calculate exponential change.

## 1.1: Bank Accounts

A bank account has a balance of \$120 on January 1. Describe a situation in which the account balance for each month (February 1, March 1, . . .) forms the following sequences. Write the first three terms of each sequence.

1. an arithmetic sequence

2. a geometric sequence

## 1.2: Shrinking a Passport Photo



The distance from Elena’s chin to the top of her head is 150 mm in an image. For a U.S. passport photo, this measurement needs to be between 25 mm and 35 mm.



1. Find the height of the image after it has been scaled by 80% the following number of times. Explain or show your reasoning.
  - a. 3 times
  - b. 6 times
  
2. How many times would the image need to be scaled by 80% for the image to be less than 35 mm?
  
3. How many times would the image need to be scaled by 80% to be less than 25 mm?



## Lesson 1 Summary

Sometimes quantities change by the same factor at regular intervals.

For example, a bacteria population might be 10,000 on the first day of measurement and then double each day after that point. This means that one day after the initial measurement, the population would be 20,000, two days after the measurement, it would be 40,000, and three days after, it would be 80,000.

The relationship can be modeled by an exponential function because the population changes by the same factor for each passing day. If  $n$  is the number of days since the bacteria population was first measured, then the population on day  $n$  is  $10,000 \cdot 2^n$ . The population is also a geometric sequence because each term is found by multiplying the previous term by 2.

days since population is measured	population
0	10,000
1	$10,000 \cdot 2$
2	$10,000 \cdot 2^2$
3	$10,000 \cdot 2^3$
$n$	$10,000 \cdot 2^n$