## Lesson 11: Prisms Practice

* Let’s calculate volumes of prisms and cylinders.

### 11.1: New Heights

Calculate the height of each solid. Round your answers to the nearest tenth if needed.

A



B



### 11.2: The Choice is Yours

Here are several solids.

A



B



C



D



E



F



G



1. Without doing any calculating, identify 2 solids you think would have the least difficult volume calculations and 2 solids that would have the most difficult volume calculations. Be prepared to explain your reasoning.
2. Choose 3 of the solids. At least 1 should be from your “least difficult” list and 1 should be from your “most difficult” list. Calculate the volumes of the solids you chose. Round your answers to the nearest tenth if needed.

#### Are you ready for more?

The images show a solid and the two-dimensional figure that was rotated to generate it.





Find 4 different positive integers for the values of $A,B,C,$ and $D$ so that the total volume of the solid is $297π$ cubic units.

### 11.3: The Cayan Tower

The building on the left side of the picture is called the Cayan Tower. It’s in the city of Dubai. The tower is about 306 meters tall. It’s made up of identical floors that are each rotated slightly compared to the one underneath it.



floor plan



Each floor is the same chevron shape that is approximately 2 parallelograms put together, with the dimensions shown in the image. The circle in the floor plan shows the cross section of the core, which is used to circulate air and carry pipes and wiring throughout the building.

1. The area of the Cayan Tower’s base is $57⋅35$ or 1,995 square meters. Why is it possible to find the area of the chevron shape by just multiplying its width and height?
2. Describe how the total volume of the building (including the core) can be calculated.
3. What shape is the core of the building, whose cross section is shown in the floor plan as a circle?
4. Describe how the volume of the building’s core can be calculated, including describing the measurements that would be used.
5. What percentage of the building’s volume is taken up by its core?

### Lesson 11 Summary

The formula $V=Bh$, where $V$ stands for volume, $B$ is the area of the base, and $h$ is the height, applies to right and oblique cylinders and all prisms. Sometimes, though, additional calculations are needed to find missing measurements before the formula can be applied.

To calculate the volume of this cylinder, first find the area of the base, which is a circle of radius 5 cm. Its area is $25π$ square centimeters. The cylinder’s height isn’t given. To find the value of the height, notice that a right triangle is formed by the 15-cm diagonal line, the 10-cm diameter of the circle, and the height of the cylinder. The diagonal line is the triangle’s hypotenuse. By the Pythagorean Theorem, $10^{2}+h^{2}=15^{2}$. That means $100+h^{2}=225$. Subtracting 100 from each side gives $h^{2}=125$, so $h=\sqrt{125}$ centimeters.



Now, the volume of the cylinder is the area of the base multiplied by the height. This is $25π⋅\sqrt{125}$ cubic centimeters, or approximately 878.1 cubic centimeters.



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