## Lesson 9: Applying Area of Circles

Let's find the areas of shapes made up of circles.

## 9.1: Still Irrigating the Field

The area of this field is about $500,000 \mathrm{~m}^{2}$. What is the field's area to the nearest square meter? Assume that the side lengths of the square are exactly 800 m .


- $502,400 \mathrm{~m}^{2}$
- $502,640 \mathrm{~m}^{2}$
- $502,655 \mathrm{~m}^{2}$
- $502,656 \mathrm{~m}^{2}$
- $502,857 \mathrm{~m}^{2}$


## 9.2: Comparing Areas Made of Circles

1. Each square has a side length of 12 units. Compare the areas of the shaded regions in the 3 figures. Which figure has the largest shaded region? Explain or show your reasoning.
A

B

C

2. Each square in Figures $D$ and $E$ has a side length of 1 unit. Compare the area of the two figures. Which figure has more area? How much more? Explain or show your reasoning.
D

E


## Are you ready for more?

Which figure has a longer perimeter, Figure D or Figure E? How much longer?

## 9.3: The Running Track Revisited

The field inside a running track is made up of a rectangle 84.39 m long and 73 m wide, together with a half-circle at each end. The running lanes are 9.76 m wide all the way around.


What is the area of the running track that goes around the field? Explain or show your reasoning.

## Lesson 9 Summary

The relationship between $A$, the area of a circle, and $r$, its radius, is $A=\pi r^{2}$. We can use this to find the area of a circle if we know the radius. For example, if a circle has a radius of 10 cm , then the area is $\pi \cdot 10^{2}$ or $100 \pi \mathrm{~cm}^{2}$. We can also use the formula to find the radius of a circle if we know the area. For example, if a circle has an area of $49 \pi \mathrm{~m}^{2}$ then its radius is 7 m and its diameter is 14 m .

Sometimes instead of leaving $\pi$ in expressions for the area, a numerical approximation can be helpful. For the examples above, a circle of radius 10 cm has area about $314 \mathrm{~cm}^{2}$. In a similar way, a circle with area $154 \mathrm{~m}^{2}$ has radius about 7 m .

We can also figure out the area of a fraction of a circle. For example, the figure shows a circle divided into 3 pieces of equal area. The shaded part has an area of $\frac{1}{3} \pi r^{2}$.


